

# Adaptive Restart Strategies for Conflict Driven SAT Solvers

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Solver	Score	#SAT	#Uns
Rsat 2007-02-08	55452	63	76
<b>picosat 535</b>	51639	72	67
minisat SAT-2007	50398	53	79
TiniSatELite 2007-02-08	49560	55	75
CMUSAT 2007-02-08	41197	46	77
MXC 2007-02-08	38004	47	69
MiraXT v3	37700	52	74
SATzilla CRAFTED	31439	47	67
SAT7 2007-02-08	27607	51	63

Solver	Score	#SAT	#Uns
SATzilla CRAFTED	74469	27	67
minisat SAT-2007	63371	26	72
MXC 2007-02-08	39848	20	57
MiraXT v3	34236	24	54
CMUSAT 2007-02-08	26461	21	45
Rsat 2007-02-08	19532	15	40
<b>picosat 535</b>	19081	22	38

# New Normalized VSIDS (NVSIDS) Reformulation of VSIDS

(consider only one variable)

feedback / punishment / I in PID:  $0 < f < 1$

$s$  old score       $s'$  new score

$$s' = \begin{cases} s \cdot f + (1 - f) & \text{if variable is involved in current conflict} \\ s \cdot f & \text{if variable is NOT involved} \end{cases}$$

$$0 \leq \underbrace{s \cdot f}_{\text{decay in any case}} \leq s' \leq \underbrace{s \cdot f + (1 - f)}_{\text{increment if involved}} \leq f + (1 - f) = 1$$

decay in any case      decay in any case      increment if involved

MiniSAT, RSAT:  $f = 0.95 \approx 1/1.05$      $(1 - f) = 0.05$

PicoSAT:  $f = 1/1.1 \approx 0.91$      $(1 - f) = 0.09$

(consider only one variable)

$$\delta_k = \begin{cases} 1 & \text{if involved in } k\text{-th conflict} \\ 0 & \text{otherwise} \end{cases}$$

$$i_k = (1 - f) \cdot \delta_k$$

$$s_n = (\dots (i_1 \cdot f + i_2) \cdot f + i_3) \cdot f \dots) \cdot f + i_n = \sum_{k=1}^n i_k \cdot f^{n-k} = (1 - f) \cdot \sum_{k=1}^n \delta_k \cdot f^{n-k} \quad (\text{NVSIDS})$$

$$S_n = \frac{f^{-n}}{(1-f)} \cdot s_n = \frac{f^{-n}}{(1-f)} \cdot (1-f) \cdot \sum_{k=1}^n \delta_k \cdot f^{n-k} = \sum_{k=1}^n \delta_k \cdot f^{-k} \quad (\text{EVSIDS})$$

- **phase saving** of assigned variables [RSAT]
  - initially pick phase according to number of occurrences
  - afterwards always pick last saved phase for decision variables
  - **rapid restarts** [TiniSAT] empirically [RSAT,PicoSAT] work nicely with phase saving
- **flipped assignment** or just **flip**
  - is a forced assignment (no decision)
  - with different previous saved phase, e.g.
    - \* last time  $x$  was assigned, it was assigned to 0
    - \* because of unit propagation  $x$  is now forced to be assigned 1

(consider only one variable)

feedback / punishment / I in PID:  $0 < g < 1$

$a$  old agility

$a'$  new agility

$$a' = \begin{cases} a \cdot g + (1 - g) & \text{if new forced assignment flips old value} \\ a \cdot g & \text{if saved phase is the same as in new assignment} \end{cases}$$

$$0 \leq \underbrace{a \cdot g}_{\text{decay in any case}} \leq a' \leq \underbrace{a \cdot g + (1 - g)}_{\text{increment if flipped}} \leq \underbrace{g + (1 - g)}_{\text{decay in any case}} = 1$$

PicoSAT:  $g = 0.9999 = 1 - 1/10000$ ,  $(1 - g) = 1/10000$

- high agility
  - measured in percentage of recent assignments that flipped variables
  - PicoSAT: at least 20% for inner restarts, at least 25% for outer restarts
  - then SAT solver is moving fast
  - with respect to Hamming distance
  - do not restart (actually do not backtrack but follow restart schedule)
- low agility
  - PicoSAT: less than 20% for inner restarts, less than 25% for outer restarts
  - SAT solver is somehow stuck
  - restart as usual

time limit 900 seconds, memory limit 1.5 GB

			industrial			crafted		
		adaptive	<i>sat</i>	<i>unsat</i>	<i>solved</i>	<i>sat</i>	<i>unsat</i>	<i>solved</i>
MiniSAT	2.0	<i>no</i>	37	57	94	22	46	68
orig. RSAT	2.0	<i>no</i>	41	51	92	10	20	30
AAS-RSAT		<i>no</i>	45	48	93	11	21	32
AAS-RSAT	25%	<b>yes</b>	44	49	93	11	24	35
AAS-RSAT	30%	<b>yes</b>	48	48	96	12	23	35
PicoSAT	741	<i>no</i>	43	54	97	14	24	38
PicoSAT	741	<b>yes</b>	44	57	101	16	<b>36</b>	52
PicoPrepSAT	143	<i>no</i>	52	58	110	21	38	59
PicoPrepSAT	143	<b>yes</b>	52	64	116	21	<b>49</b>	70

- new metric ANRFA to measure agility / velocity of search
  - reformulated VSIDS as control problem (NVSIDS)
  - applied same “controller” to flipped assignments
  - came up with good magic constants:  $g = 0.9999$  20% 25%
- prohibit restarts if SAT solver is not moving fast enough
  - are there better metrics than ANRFA?
  - does ANRFA capture velocity with respect to Hamming distance good enough?
- so far failed to extend these ideas to other magic constants
  - average recently used learned clauses can be calculated in the same way
  - goal is to control reduce schedule resp. garbage collection schedule