

Group: \_\_\_\_\_

Assignment 8

Name: \_\_\_\_\_

Formal Models

Matr.Nr.: \_\_\_\_\_

Summer Semester 2010

Points: \_\_\_\_\_

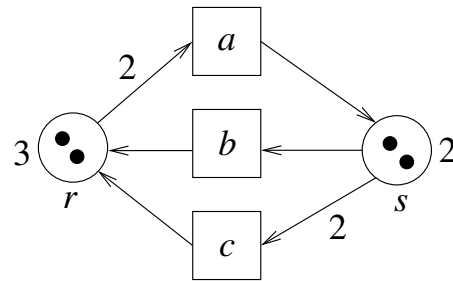
Due: 27.05.2010 08:30

Institute for Formal Models and Verification, Dr. Robert Brummayer, Dipl.-Ing. Florian Lonsing

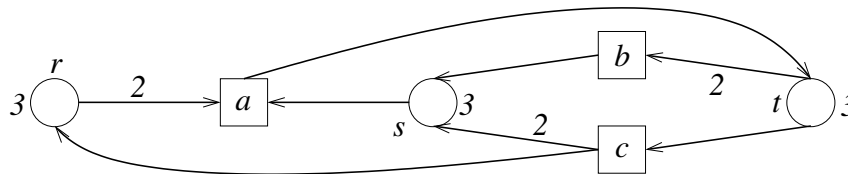
### Exercise 29

Given PTN  $N$  as shown on the right. *Justify* your answers to the following questions.

- Specify  $N$  formally as 5-tuple  $N = (P, I, T, G, C)$  including all of its components.
- How many different markings are possible in  $N$  *theoretically*?
- Is there a marking  $M$  for  $N$  such that all transitions are enabled?



### Exercise 30



Given PTN  $N$  as shown above. *Justify* your answers to the following questions.

- How many different markings are possible in  $N$  *theoretically*?
- Given markings  $M_1 = \{(r, 1), (s, 3), (t, 1)\}$ ,  $M_2 = \{(r, 1), (s, 2), (t, 1)\}$ ,  $M_3 = \{(r, 2), (s, 2), (t, 1)\}$  and  $M_4 = \{(r, 2), (s, 1), (t, 1)\}$ . Determine the set of all transitions which are enabled in  $M_1$ ,  $M_2$ ,  $M_3$  and  $M_4$ , respectively.
- Given marking  $M = \{(r, 2), (s, 1), (t, 2)\}$ . For all transitions  $t$  enabled in  $M$ , determine marking  $M'$  obtained from firing  $t$  in  $M$ .

### Exercise 31

Draw the LTS for PTN  $N$  from Exercise 29 with the initial marking as given in the figure.

### Exercise 32

- a) Transform  $\neg\forall x. (\phi \rightarrow \psi)$  into  $\exists x. (\phi \wedge \neg\psi)$  and specify all intermediate steps.
- b) Reformulate  $\forall x. (\phi \leftrightarrow \psi)$  using only  $\exists$  and operators  $\neg$  and  $\wedge$ . Specify all intermediate steps.
- c) Explain in your own words the effects of reordering quantifiers. More precisely, explain the semantical difference between  $\forall x\exists y. \phi$  and  $\exists y\forall x. \phi$  in general.