

# Formal Models SS 2012: Assignment 2

Institute for Formal Models and Verification, JKU Linz

Due 22.03.2012

## Exercise 5

Draw an FA  $A$  with input-alphabet  $\Sigma := \{a, b\}$  having *exactly* 3 states such that...

1. ... $A$  is non-deterministic and incomplete.
2. ... $A$  is deterministic and incomplete.
3. ... $A$  is non-deterministic and complete.
4. ... $A$  is deterministic and complete.

Justify each of your solutions.

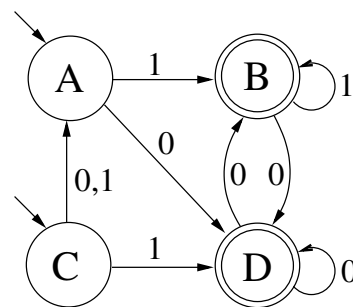
## Exercise 6

Let  $A_1$  be an *arbitrary* FA and  $\mathbb{P}(A_1) := (S, I, \Sigma, T, F)$  be the power automaton of  $A_1$ . Describe in your own words the formal definition of  $\mathbb{P}(A_1)$ , including all of its components. Is the following proposition true? Justify your answer.

$$|S' \xrightarrow{a}| = 1 \text{ for all } S' \in S \text{ and for all } a \in \Sigma.$$

## Exercise 7

Draw the power automaton  $\mathbb{P}(A)$  for FA  $A$  as shown on the right. What is the maximum number of states  $\mathbb{P}(A)$  can have in theory? Justify your answer.



## Exercise 8

Draw a *deterministic* FA  $A$  with  $\Sigma := \{a, b\}$  having *at least* 3 states such that  $L(C(A)) \neq \overline{L(A)}$ , where  $C(A)$  denotes the complement-automaton of  $A$ . Explain your solution.

## **Bonus Exercise**

Reimplement the program available at

`http://fmv.jku.at/fm/faimpl.zip`

in your favorite object-oriented language (Java, C#, C++, ...) using the "objects for states"-pattern. Please ensure that you bring it in electronic form (USB stick, laptop) for the presentation.