

On the Complexity of Fixed-Size Bit-Vector Logics with Binary Encoded Bit-Width

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- How does the encoding of the bit-widths affect the complexity of satisfiability checking for BV logics?
- In practice logarithmic (e.g. binary, decimal, hexadecimal) encoding is used (in contrast to unary encoding)

Example in SMT2

```
(set-logic QF_BV)
(declare-fun x () (_ BitVec 1000000))
(declare-fun y () (_ BitVec 1000000))
(assert (distinct (bvadd x y) (bvadd y x)))
```

Using Boolector:

- 103 MB in AIGER format; 1 GB in DIMACS format
- Bit-width of 10 million → cannot be bit-blasted (due to integer overflow)

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<u>no</u>		<u>yes</u>	
uninterpreted functions		uninterpreted functions	
<u>no</u>	<u>yes</u>	<u>no</u>	<u>yes</u>
QF_BV	QF_UFBV	BV	UFBV

		quantifiers			
		<u>no</u>		<u>yes</u>	
		uninterpreted functions		uninterpreted functions	
		<u>no</u>	<u>yes</u>	<u>no</u>	<u>yes</u>
encoding	<u>unary</u>	QF_BV1	QF_UFBV1	BV1	UFBV1
	<u>binary</u>	QF_BV2	QF_UFBV2	BV2	UFBV2

Assume common (SMT-LIB) operators \rightarrow bit-blasting is polynomial in bit-width

Complexity: completeness results

		QF_BV	QF_UFBV	BV	UFBV
encoding	<u>unary</u>	?	?	?	?
	<u>binary</u>	?	?	?	?

- QF_BV1 is NP-complete ← bit-blasting to SAT
- QF_UFBV1 is NP-complete ← using Ackermann constraints
- BV1 is PSPACE-complete ← bit-blasting to QBF
- UFBV1 is NEXPTIME-complete ← proved in:
 - C. M. Wintersteiger, *Termination Analysis for Bit-Vector Programs*. PhD Thesis, ETH Zürich, 2011.
 - C. M. Wintersteiger, Y. Hamadi, L. Mendonça de Moura, *Efficiently Solving Quantified Bit-Vector Formulas*. Proc. FMCAD, 2010.

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QF_BV2 is NEXPTIME-complete:

- QF_BV2 \in NEXPTIME:

$$\text{QF_BV2} \xrightarrow{\text{exponentially}} \text{QF_BV1} \in \text{NP}$$

- QF_BV2 is NEXPTIME-hard:

$$\text{DQBF} \xrightarrow{\text{polynomially}} \text{QF_BV2}$$

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Dependency Quantified Boolean Formulas (DQBF):

- Applying Henkin quantifiers: variable dependencies represent a partial order
- Dependencies are explicitly specified

Example DQBF

$$\forall u_0, u_1, u_2 \exists x(u_0), y(u_1, u_2) . (x \vee y \vee \neg u_0 \vee \neg u_1) \wedge$$

$$(x \vee \neg y \vee u_0 \vee \neg u_1 \vee \neg u_2) \wedge$$

$$(x \vee \neg y \vee \neg u_0 \vee \neg u_1 \vee u_2) \wedge$$

$$(\neg x \vee y \vee \neg u_0 \vee \neg u_2) \wedge$$

$$(\neg x \vee \neg y \vee u_0 \vee u_1 \vee \neg u_2)$$

- DQBF is NEXPTIME-complete
G. L. Peterson, J. H. Reif, *Multiple-Person Alternation*. Foundations of Computer Science, 1979.

$$\left((X^{[8]} \mid Y^{[8]} \mid \sim U_0^{[8]} \mid \sim U_1^{[8]}) \ \& \ (X \mid \sim Y \mid U_0 \mid \sim U_1 \mid \sim U_2^{[8]}) \ \& \right. \\
(X \mid \sim Y \mid \sim U_0 \mid \sim U_1 \mid U_2) \ \& \ (\sim X \mid Y \mid \sim U_0 \mid \sim U_2) \ \& \\
\left. (\sim X \mid \sim Y \mid U_0 \mid U_1 \mid \sim U_2) \right) = \sim 0^{[8]}$$

- 1 Eliminate the quantifier prefix
- 2 Replace logical connectives with bit-wise operators
- 3 Replace Boolean variables with bit-vector variables of bit-width 2^k
 k : number of universal variables in the DQBF

$$\begin{aligned} & \left((X^{[8]} \mid Y^{[8]} \mid \sim U_0^{[8]} \mid \sim U_1^{[8]}) \ \& \ (X \mid \sim Y \mid U_0 \mid \sim U_1 \mid \sim U_2^{[8]}) \ \& \right. \\ & (X \mid \sim Y \mid \sim U_0 \mid \sim U_1 \mid U_2) \ \& \ (\sim X \mid Y \mid \sim U_0 \mid \sim U_2) \ \& \ \\ & \left. (\sim X \mid \sim Y \mid U_0 \mid U_1 \mid \sim U_2) \right) = \sim 0^{[8]} \end{aligned}$$

4 Universal vars \leftarrow Assign binary magic numbers to U_i !

$$U_0 := \begin{bmatrix} 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \\ 0 \\ 1 \end{bmatrix}, \quad U_1 := \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{bmatrix}, \quad U_2 := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

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$$U_i := \frac{2^{(2^k)} - 1}{2^{(2^i)} + 1}$$

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5 Existential vars \leftarrow Represent Skolem-functions as bit-vectors!

$$X = \begin{bmatrix} x_7 \\ x_6 \\ x_5 \\ x_4 \\ x_3 \\ x_2 \\ x_1 \\ x_0 \end{bmatrix} \text{ is independent of } U_1 = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{bmatrix}$$

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Positive and negative cofactors of a Skolem-function w.r.t. U_i

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X is independent of U_i :

$$(X \ \& \ U_i) = ((X \ \gg \ (1 \ll i)) \ \& \ U_i)$$

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$$\wedge (Y \& U_0) = ((Y \gg (1 \ll 0)) \& U_0)$$

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Bit-width 2^k is encoded logarithmically, due to binary encoding!

Complexity: completeness results

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encoding	<u>unary</u>	NP	NP	PSPACE	NEXPTIME
	<u>binary</u>	NEXPTIME	?	?	?

- QF_UFBV2 is NEXPTIME-complete ← using Ackermann constraints
- BV2 \in EXPSPACE and is NEXPTIME-hard
- UFBV2 is 2-NEXPTIME-complete:

$2^{(2^n)}$ -square domino tiling problem $\xrightarrow{\text{polynomially}}$ UFBV2

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Bit-width bounded problems

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	<u>binary</u>	NEXPTIME	NEXPTIME	?	2-NEXPTIME

- Bit-width boundedness: a practical property for BV problems to avoid exponential blow-up
- If a BV problem S is bit-width bounded:
 - $S \subset \text{QF_BV}(2) \Rightarrow S \in \text{NP}$
 - $S \subset \text{QF_UFBV}(2) \Rightarrow S \in \text{NP}$
 - $S \subset \text{BV}(2) \Rightarrow S \in \text{PSPACE}$
 - $S \subset \text{UFBV}(2) \Rightarrow S \in \text{NEXPTIME}$

		QF_BV	QF_UFBV	BV	UFBV
encoding	<u>unary</u>	NP	NP	PSPACE	NEXPTIME
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- Restriction on operators:
 - $\text{QF_BV}(2)_{bw+eq}$ is NP – *complete*
 - $\text{QF_UFBV}(2)_{bw+eq}$ is NP – *complete*
 - slicing, concatenation, shifts, addition, or multiplication
 \Rightarrow NEXPTIME – *complete*
- Restriction on bit-width of universal variables:
 - $\text{BV}(2)_{log}$ is NEXPTIME – *complete*
 - $\text{UFBV}(2)_{log}$ is NEXPTIME – *complete*

Conclusion

		QF_BV	QF_UFBV	BV	UFBV
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	<u>binary</u>	NEXPTIME	NEXPTIME	?	2-NEXPTIME

The complexity of deciding the commonly used BV logics was an open question.

Future work:

- Is BV2 complete?
- Consider these results in the context of parametrized complexity
- Instead of bit-blasting+SAT, other approaches with EPR/DQBF?

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