# Formal Models SS 2015: Assignment 7 

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## Exercise 25

Let $N=(C, I, E, G)$ be the following CEN:
$C=\{r, s, u, v, w, x\}, I=\{r, u, w\}, E=\{b, c, d, e\}$,
$G=\{(r, b),(b, s),(s, c),(c, r),(c, u),(u, b),(b, v),(v, d),(d, x),(x, e),(e, w),(w, d)\}$

- Draw $N$. How many markings for $N$ are possible theoretically?
- Let $M$ be a marking of $N$ with $M=\{r, s, u\}$. Which are the events that can fire in $M$ ? What are the possible new markings obtained from this?
- Let $M$ be a marking of $N$ with $M=\{r, u, v, w\}$. Which are the events that can fire in $M$ ? What are the possible new markings obtained from this?
- Let $M$ be a marking of $N$ with $M=\{s, u, x\}$. Which are the events that can fire in $M$ ? What are the possible new markings obtained from this?
- Draw the LTS corresponding to $N$.

Exercise 26 Let $N$ be the PTN shown below.


- Specify $N$ formally as a 5-tuple $N=(P, I, T, G, C)$. How many markings for $N$ are possible theoretically?
- Now let $M$ be a marking of $N$ with $M(r)=0, M(s)=1, M(t)=2$. Which are the transitions that can fire in $M$ ? What are the possible new markings obtained from this?
- Is there a marking for $N$ so that all transitions are enabled? Justify your answer!


## Exercise 27



Given PTN $N$ as shown above. Justify your answers to the following questions.
a) How many different markings are possible in $N$ theoretically?
b) Given markings $M_{1}=\{(r, 1),(s, 3),(t, 1)\}, M_{2}=\{(r, 1),(s, 2),(t, 1)\}, M_{3}=\{(r, 2),(s, 2),(t, 1)\}$ and $M_{4}=\{(r, 2),(s, 1),(t, 1)\}$. Determine the set of all transitions which are enabled in $M_{1}$, $M_{2}, M_{3}$ and $M_{4}$, respectively.
c) Given marking $M=\{(r, 2),(s, 1),(t, 2)\}$. For all transitions $t$ enabled in $M$, determine marking $M^{\prime}$ obtained from firing $t$ in $M$.

## Exercise 28

Let $N=(P, I, T, G, C)$ be a PTN specified by the following sets:
$P=\{r, s\}, I=\{(r, 1),(s, 2)\}, T=\{a, b, c\}$,
$G=\{(r, a),(r, b),(a, s),(b, s),(s, c),(c, r)\}$,
$C=\{(r, 3),(s, 2)\} \cup\{(r, a, 1),(r, b, 1),(a, s, 2),(b, s, 1),(s, c, 2),(c, r, 1)\}$

- Draw $N$. How many different markings are possible on $N$ theoretically?
- Draw the LTS corresponding to $N$.

